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# Vehicle Self-Localization with High-Precision Digital Maps

Fahrzeugeigenlokalisierung mit hochgenauen digitalen Karten

**Florian Janda, Andreas Schindler**  
FORWISS, Universität Passau



Supported by:



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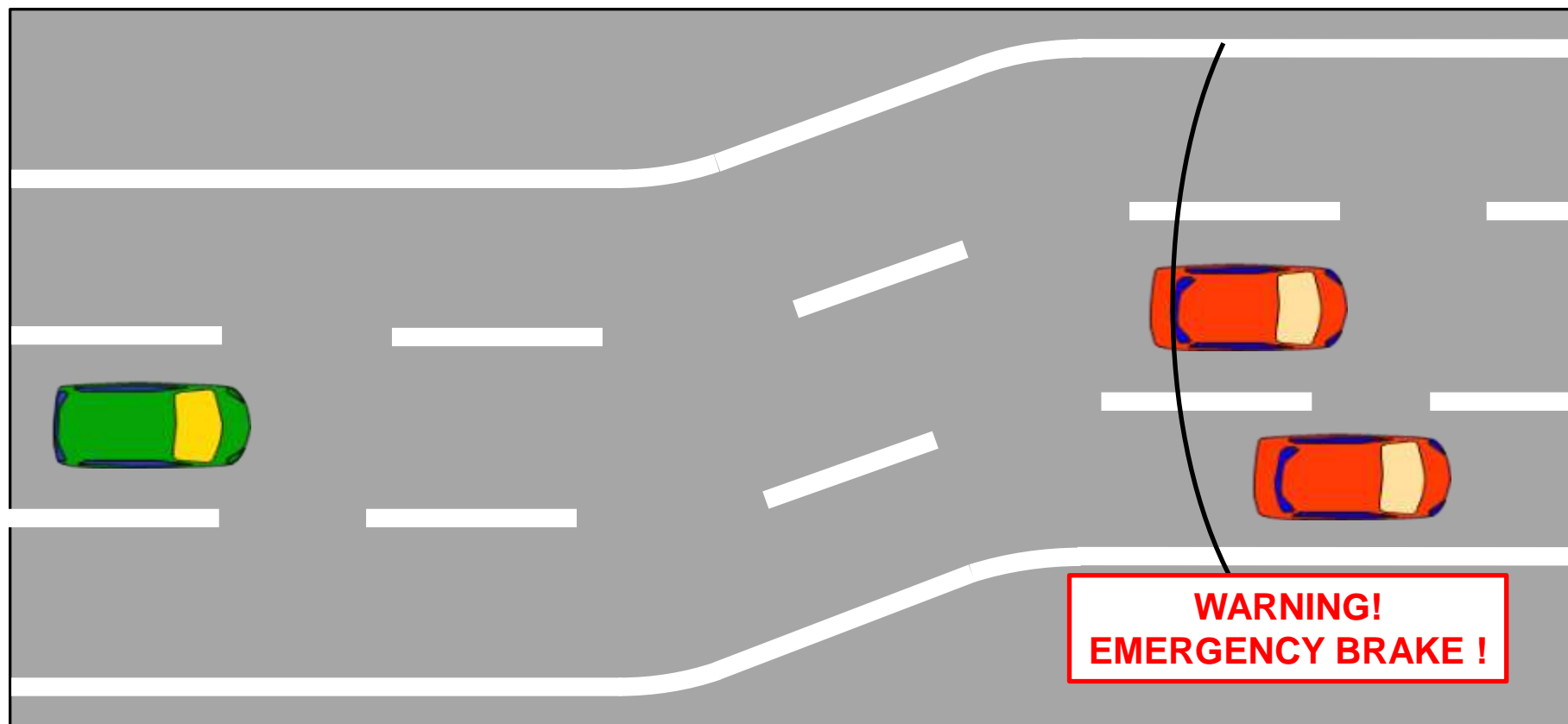
- Cooperative ADAS require precise localization strategies
- Global accuracy below 1m
  - Association of vehicles and lanes
  - Consistent integration of environment models



# Motivation for self-localization



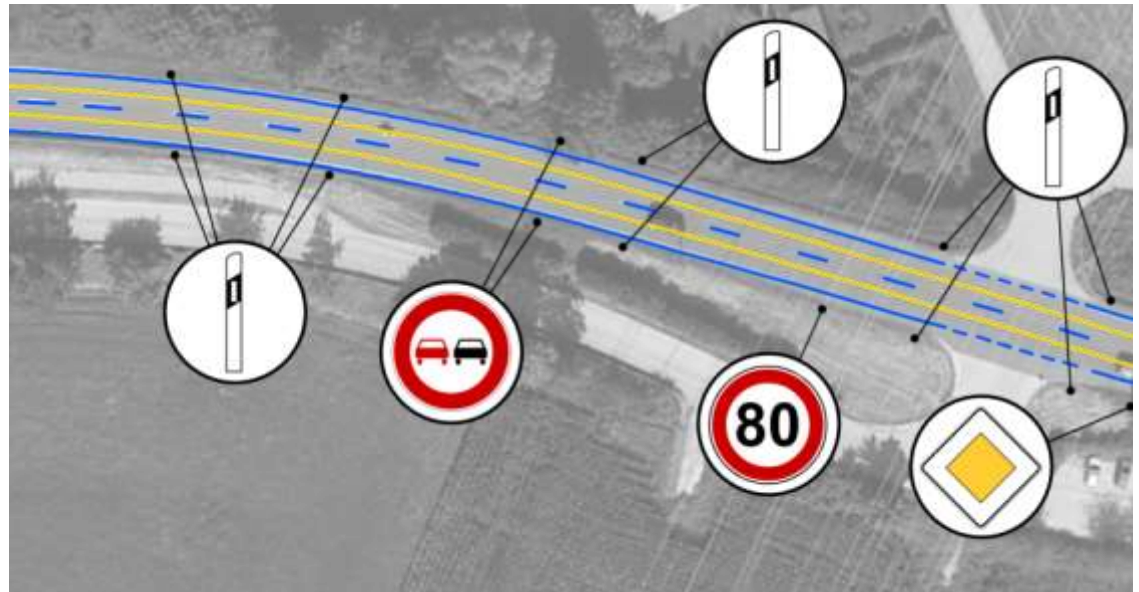
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# High-Precision Digital Maps

## Elements:

- Individual lanes (including elevation profile)
- Landmarks
  - Road markings
  - Traffic signs
  - Trees



## Requirements:

- High global accuracy
- Compact representation
- Efficient calculations / usage of map elements

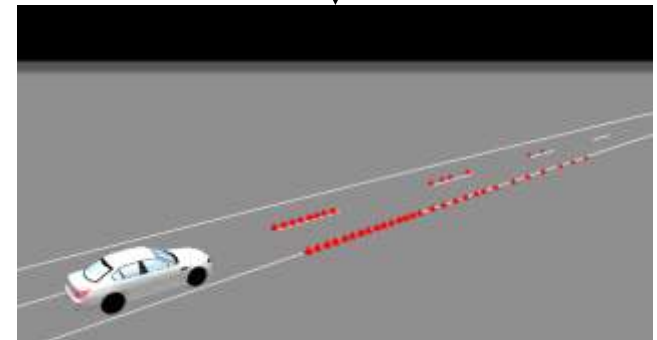
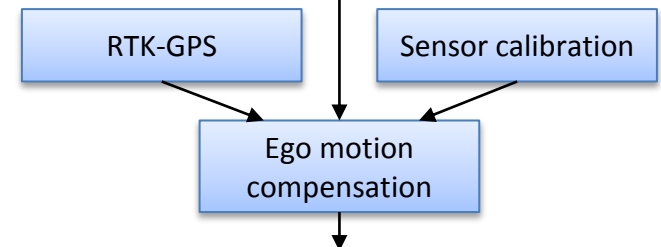
- Estimation of local road model parameters
- Video based extraction of measuring points on road markings

- Reconstruction in
  - vehicle frame

$$P^{(V)} \subset \mathbb{R}^2 \quad (\rightarrow \text{Localization})$$

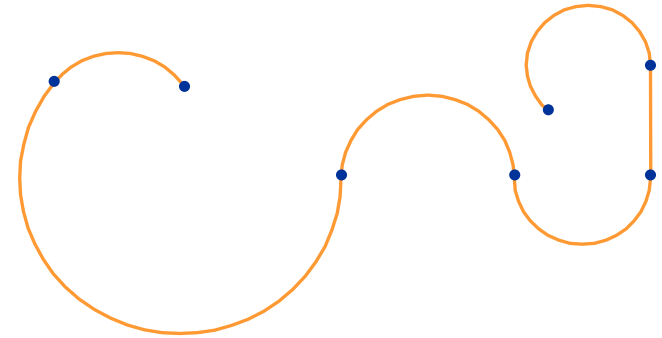
- world frame using RTK-GPS data

$$P^{(W)} \subset \mathbb{R}^2 \quad (\rightarrow \text{Mapping})$$



# Smooth circular arc splines

- Curve composed by **circular arcs** and **line segments**
- Smooth transition at breakpoints ( $G^1$  continuity)



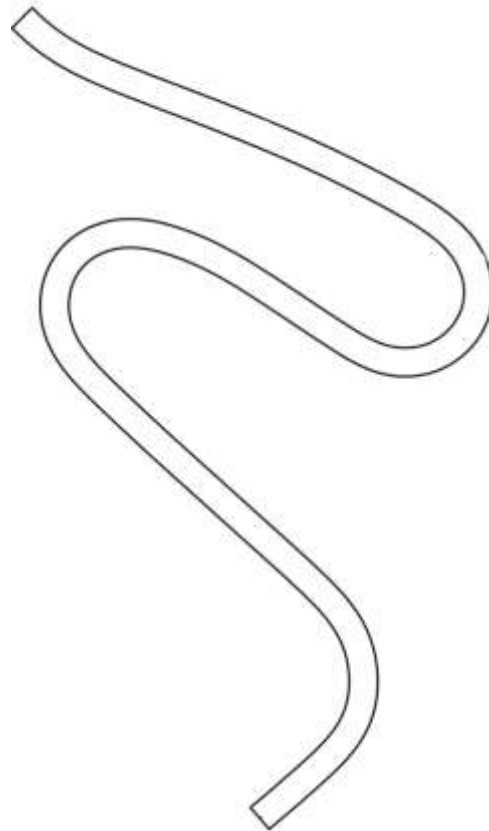
## Properties:

- Invariant wrt. rotation, translation and isotropic scaling
- Exact and direct calculation of curve length and offset curves
- Distance calculation to segments in closed form
- Compatibility with CAD and GIS systems

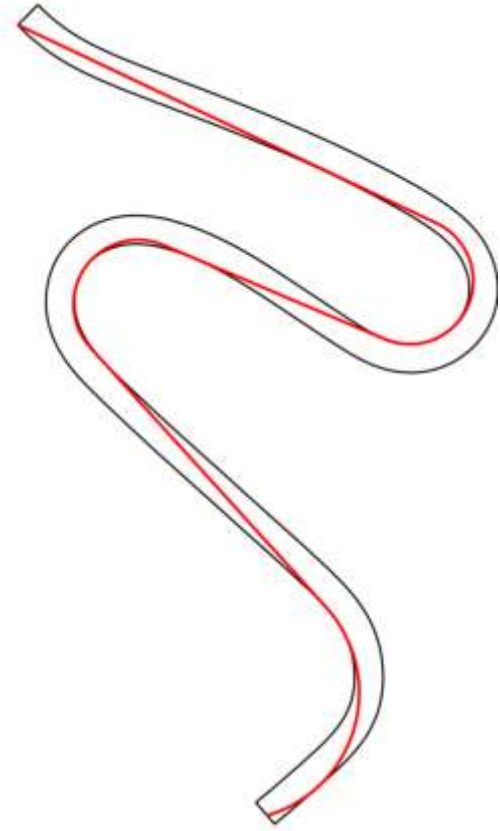
# Arc spline approximation: Smooth Minimum Arc Path



- Controllable accuracy
- Minimal segment number



**SMAP**  
→

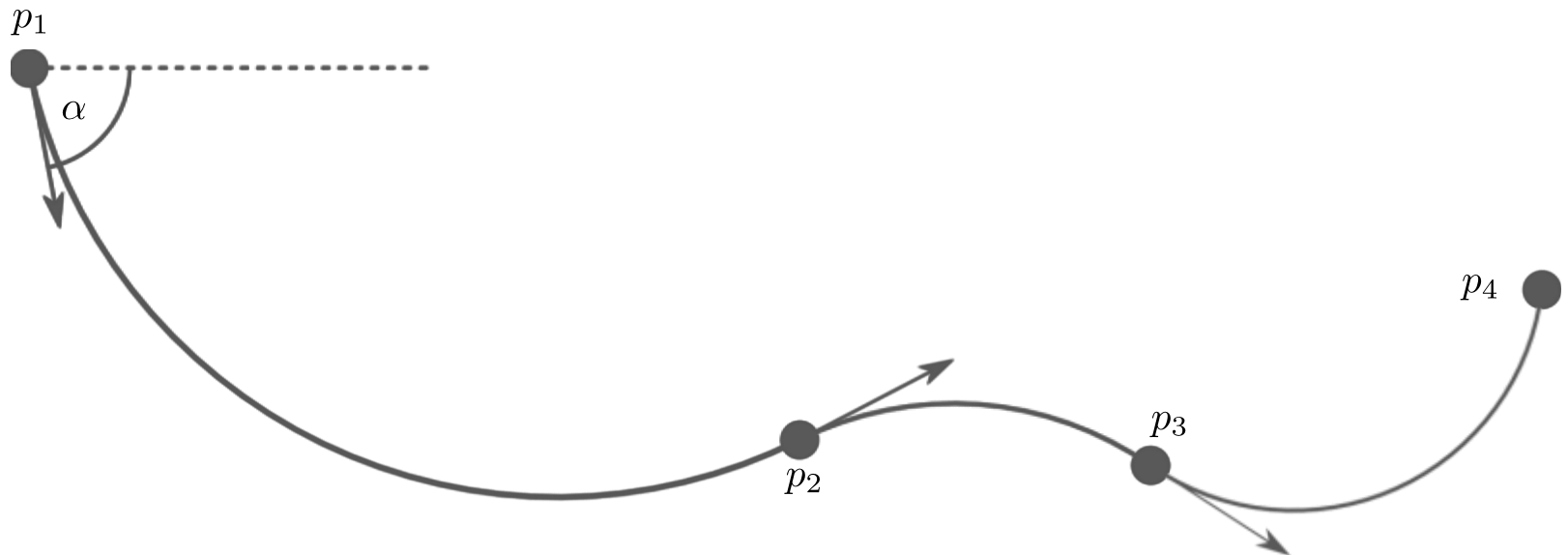




# Data volume of Smooth Arc Splines as compared to Polylines



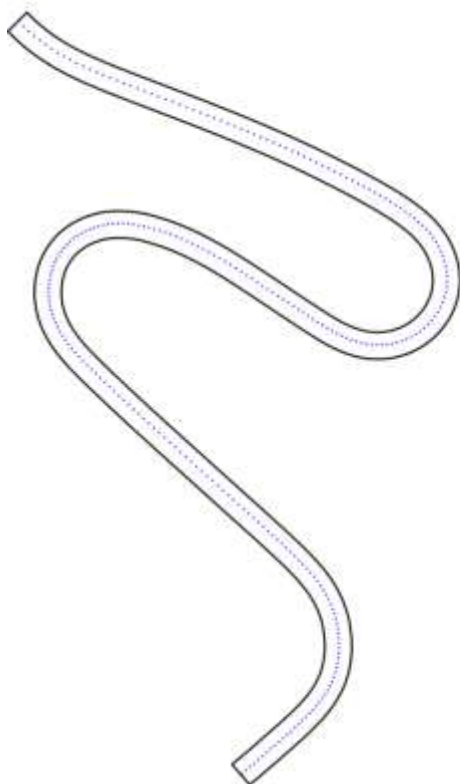
Any smooth arc spline with  $n$  segments can be encoded using  $2n + 3$  floating points (or fixed points)  
(In comparison: Any polygon requires  $2n + 2$  floating points)



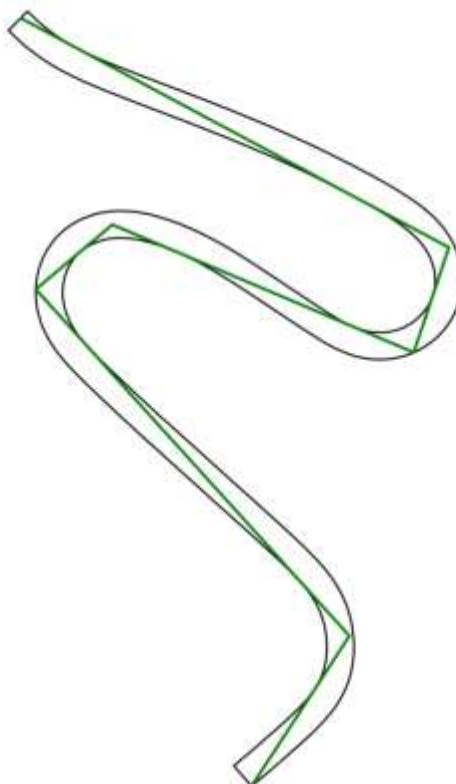
# MLP vs. SMAP



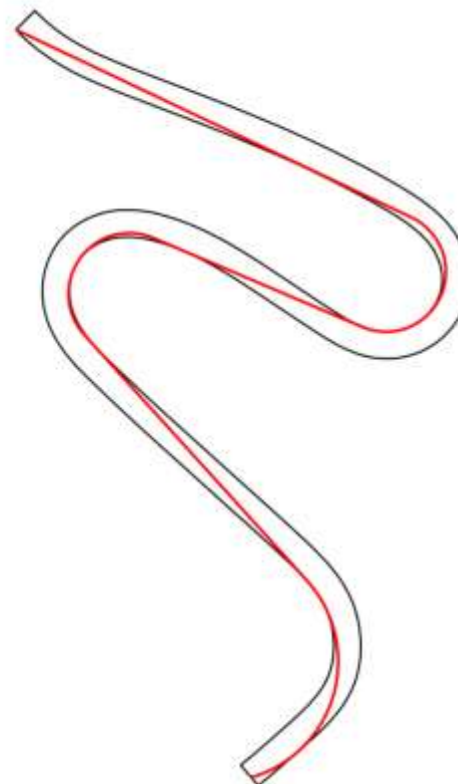
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Point sequence



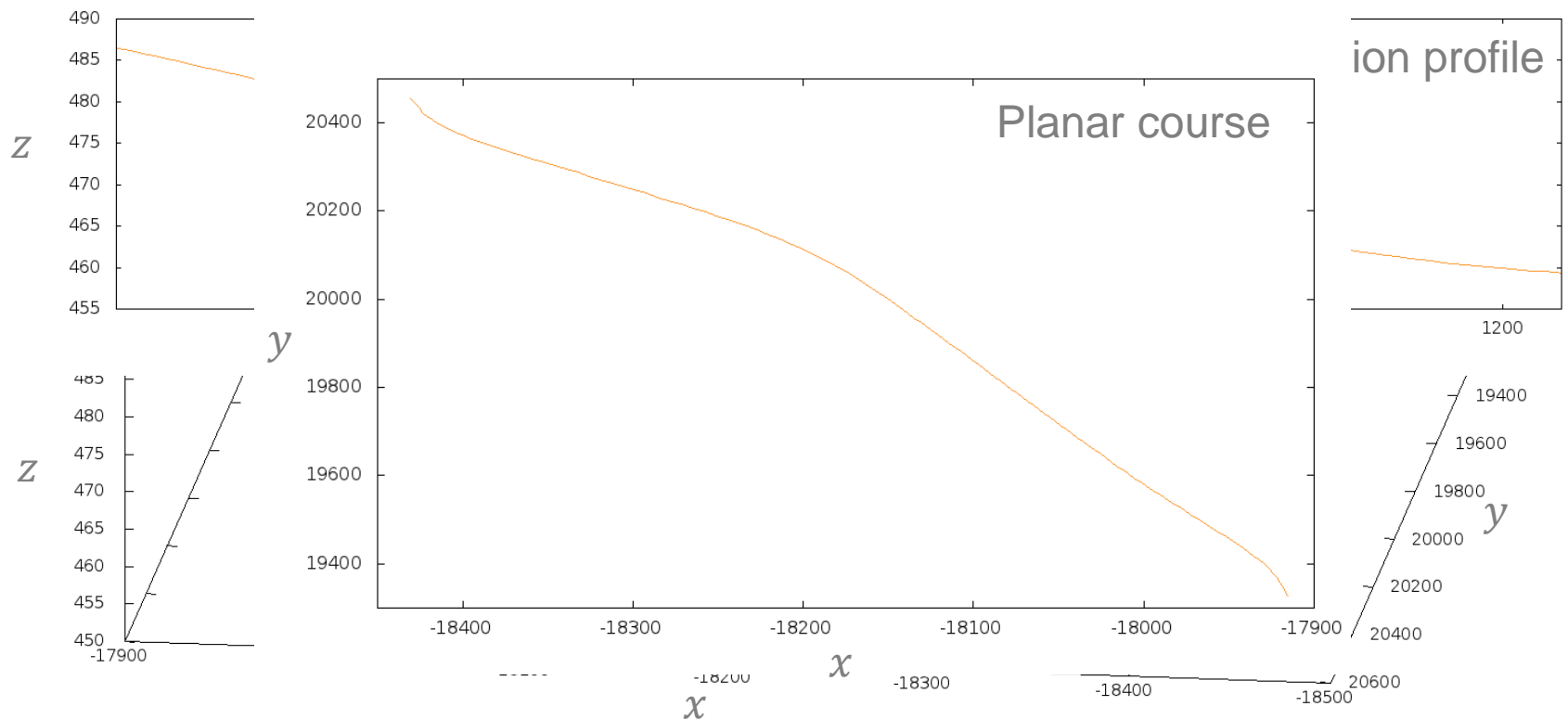
Minimum Link Path  
(MLP)



Smooth Minimum Arc Path  
(SMAP)

# 3D representation of lanes

## Planar arc spline with separated elevation profile



# Rural example map north of Munich

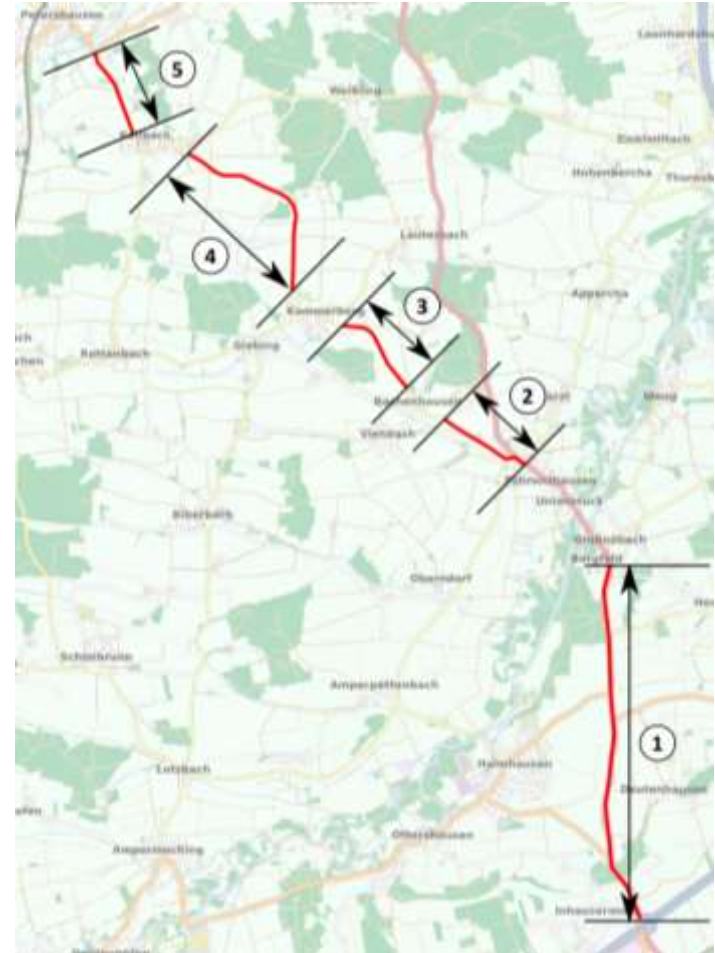
- Statistics:

- Total length: ca. 24 km
- $\emptyset$  segment length: ca. 70 m
- Max segment length: ca. 316 m
- Landmarks: ca. 2800

- Achieved global accuracy:

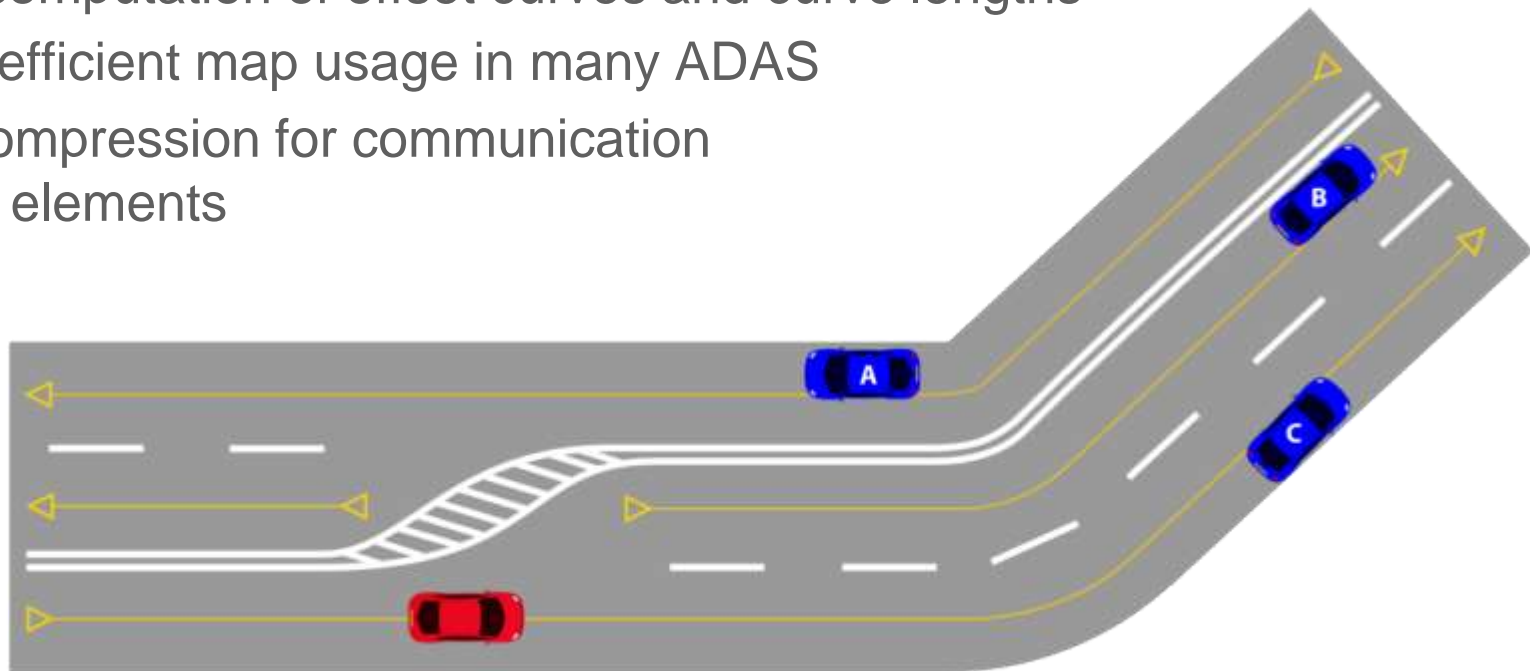
- Road markings: ca. 10 cm
- Landmarks: ca. 30 cm

Evaluated and verified through independent high-precision reference measurements.



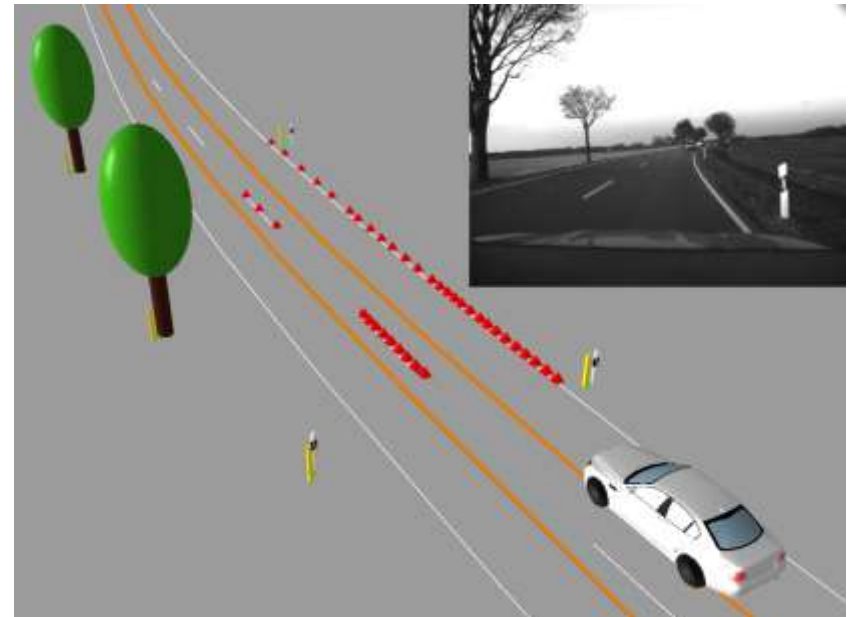
The proposed map model offers:

- 2D and 3D representation of roads and lanes
- Approximation with preset (and therefore controlled) accuracy
- Exact computation of offset curves and curve lengths
- Highly efficient map usage in many ADAS
- High compression for communication of map elements



# Vehicle Self-Localization

Association of **landmarks** (road markings, traffic signs, trees) with elements of a **high-precision digital map** in order to estimate the vehicle's position and orientation



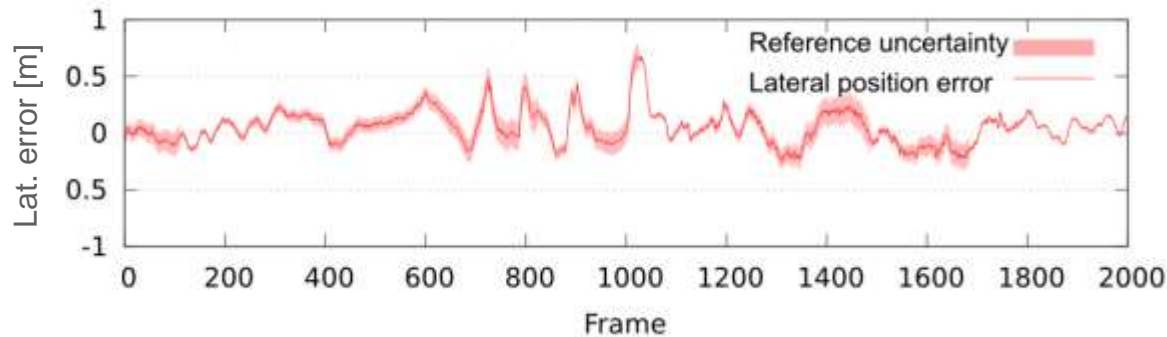
- **System state at time  $t_k$ :**

$$\mathbf{x}_k = \begin{pmatrix} x_k \\ y_k \\ \varphi_k \\ v_k \\ \dot{\varphi}_k \\ \beta_k \end{pmatrix} = \begin{pmatrix} \text{Position } x \\ \text{Position } y \\ \text{Orientation} \\ \text{Velocity} \\ \text{Yaw rate} \\ \text{Slip angle} \end{pmatrix}$$

- **Dynamic model (CTRV):**
- **Observation models:**
  - GPS (initialization)
  - Point landmarks
  - Continuous landmarks
- **Sequential Monte Carlo method** with  $M$  particles
- **Prototype fitting** to solve the landmark association problem

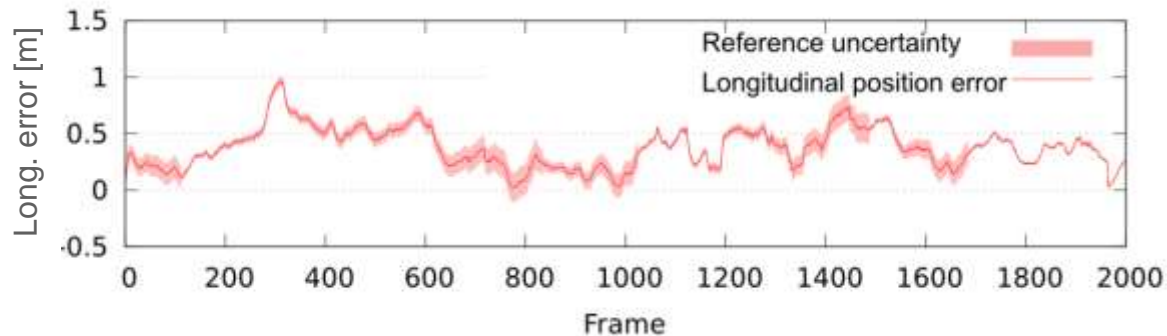


# Positioning results

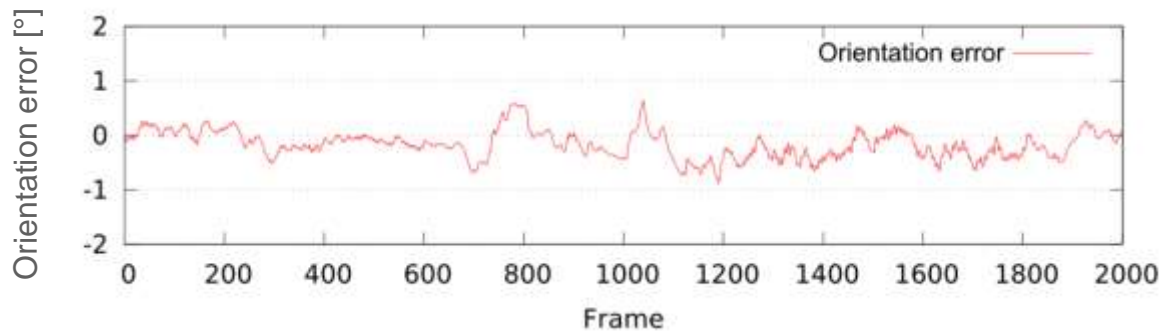


Mean and standard deviation  
of absolute errors:

$$\mu = 0,12m \quad \sigma = 0,10m$$



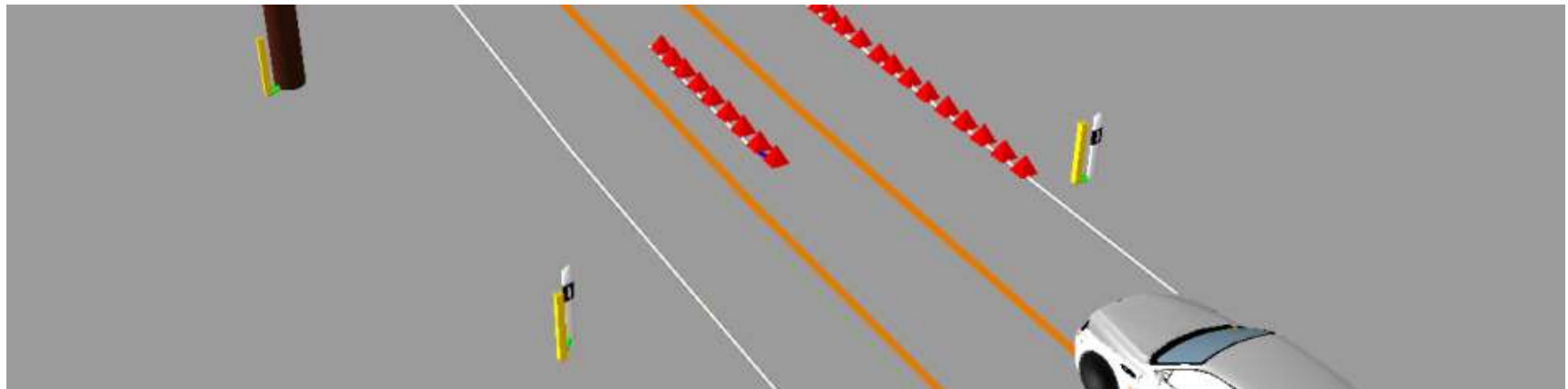
$$\mu = 0,38m \quad \sigma = 0,17m$$



$$\mu = 0,25^\circ \quad \sigma = 0,18^\circ$$

## The proposed localization strategy offers:

- **Global positioning accuracy**  $< 1\text{m}$
- **Global orientation accuracy**  $< 1^\circ$
- **Full real-time capability:** cycle time  $< 10\text{ms}$
- Positioning strategy benefits extensively from the positive properties of the **arc spline map model**



# Demonstration

Ko-PER

# Generation of high precision maps

FORWISS, University of Passau



aufgrund eines Beschlusses  
des Deutschen Bundestages

Thank you for your attention!